

NATIONAL SENIOR CERTIFICATE

GRADE 11

NOVEMBER 2016

MATHEMATICS P1

MARKS: 150

TIME: 3 hours



This question paper consists of 6 pages.

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of NINE questions. Answer ALL the questions.
- 2. Clearly show ALL calculations, diagrams, graphs, et cetera that you have used in determining your answer.
- 3. You may use an approved scientific calculator (non-programmable and nongraphical), unless stated otherwise.
- 4. Answers only will not necessarily be awarded full marks.
- 5. If necessary, round off answers to TWO decimal places, unless stated otherwise.
- 6. Diagrams are NOT necessarily drawn to scale.
- 7. Number the answers correctly according to the numbering system used in this question paper.
- 8. Write neatly and legibly.
- 9. An information sheet with formulae is included at the end of the question paper.

[21]

QUESTION 1

1.1 Solve for *x*.

1.1.1 $(x+2)^2 = 1$ (3)

$$1.1.2 \quad 2x^2 - 11x - 4 = 0 \tag{4}$$

1.1.3
$$x^2 > \frac{1}{4} \text{ and } x < 0$$
 (4)

1.1.4
$$x + 5 = \sqrt{(3 - 3x)}$$
 (4)

1.2 1.2.1 Factorise:
$$y^2 - 9x^2$$
 (1)

1.2.2 Hence or otherwise solve the following equations simultaneously:

$$y + 3x = 2$$
 and $y^2 - 9x^2 = 16$ (5)

QUESTION 2

2.1 Simplify:

$$2.1.1 \quad \left(\frac{a^3}{2}\right)^2 \tag{1}$$

2.1.2
$$\frac{2^{x-3}-3.2^{x-1}}{2^{x-2}}$$
 (4)

- 2.2 Find the value of: 10^{x+3} if $10^x = 1,5$ (2)
- 2.3 Solve for *x*:

2.3.1 $2^x = 0,125$ (2)

2.3.2
$$0,5^x$$
. $\sqrt{1 + \frac{9}{16}} = 10$ (5)

QUESTION 3

3.1	For which value(s) of <i>m</i> will the equation $2x(x + 1) + m = x$ have non-real roots?	(5)
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3.2 If:
$$f(x) = \frac{\sqrt{x+2}}{5-x^2}$$

For which value(s) of x is f(x) not defined?

(5) [**10**]

QUESTION 4

4.1	Given the sequence: 7 ; 12; 17;						
	4.1.1	Write down the next two terms of the sequence.	(2)				
	4.1.2	Determine the general term of the sequence in the form of $T_n = an + b$. (2)					
	4.1.3	Determine if 12^5 will be a term in above sequence. (3)					
	4.1.4	Explain why any positive number ending with a 2 will form part of the sequence.	(2)				
4.2	Given	the sequence: 3;9;17;27;					
	4.2.1	Write down the value of the next term of the sequence.	(1)				
	4.2.2	Determine an expression for the $\mathbf{n}^{\mathbf{th}}$ term of the sequence.	(5)				
	4.2.3	Calculate the value of the first term that is greater than 269.	(4)				
4.3	A quadratic pattern has a second term equal to 6 , a third term equal to 2 and a fifth term equal to -18 .						
	4.3.1	Calculate the second difference of the pattern.	(4)				
	4.3.2	Calculate the first term.	(3) [26]				
QUES	STION	5					
Given	:	$f(x) = \frac{8}{x-8} + 4$					
5.1	Write down the equations of the asymptotes of f .						
5.2	Write down the domain and range of f .						
5.3	Draw the graph of f showing all intercepts and asymptotes.						
5.4	Use y	our graph to solve for x, if :	(2)				
	5.4.1	$\frac{8}{x-8} \ge -4$	(3)				
	5.4.2	$f(x) \leq 3$	(3)				
5.5	Determine the equation of the positive axis of symmetry of f .						
5.6	Determine the equation of g if $g(x) = f(x - 2) - 2$.						

QUESTION 6

Sketched below are the graphs of $f(x) = ax^2 + bx + c$ and $g(x) = k \cdot m^x$. The parabola has intercepts (-5; 0); (-1; 0) and (0; 2). The exponential graph passes through the points (0; 2) and (1; 6).



6.1	Determine the equation of the parabola in the form of $y = ax^2 + bx + c$.								
6.2	Determine the values of m and k .								
6.3	Write down the equation of the asymptote of the exponential curve.								
6.4	Determine the value(s) of x for which:								
	6.4.1	f(x) is decreasing	(2)						
	6.4.2	$2 \le g(x) \le 6$	(2)						
	6.4.3	$g(x) \leq 2$	(2)						
	6.4.4	f(x).g(x)<0	(2)						
6.5	Determine the average gradient between the points $(-5; 0)$ and the y-intercept of g .								
QUI	QUESTION 7								
The graph of $y = b^x$ is shifted 2 units to the right and 4 units upwards. The shifted graph passes through the point (4;8).									
71	Calculate the value of b								

7.1 Calculate the value of
$$\boldsymbol{b}$$
. (4)

7.2Hence, write down the equation of shifted graph.(1)[5]

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QUESTION 8

			TOTAL:	150			
		(b)	The pupil does not participate in sport and is not female?	(1) [20]			
		(a)	It is a girl and participates in sport?	(1)			
	9.3.2	What is the probability that if a grade 8 pupil is chosen at random that:					
	9.3.1	Complete a two way contingency table for the above survey.					
9.3	A survey was conducted amongst 60 boys and 60 girls in grade 8 relating to their participation in sport. 20 girls did not participate in any sport and 50 boys did participate in a sport.						
	9.2.2	A green and a pink sweet are selected		(5)			
	9.2.1	Both sweets are blue					
9.2	Determ	probability that: (Round of your answer to three decimal places)					
9.1	Draw a	a tree diagram to determine all possible outcomes.					
A paci succes	ket of sw ssion fro	veets com m the pa	ntains 3 pink, 2 green and 5 blue sweets. Two sweets are removed in acket without replacing them.				
QUES	STION 9	9					
	8.3.3	Suppo makes 4 year	ose John invest his money for a total of 4 years, but after 18 months he is a withdrawal of R 20 000. How much will he receive at the end of rs?	(4) [17]			
	8.3.2	Use th he inv	he effective interest rate to calculate the value of John's investment if rested the money for 3 years.	(3)			
	8.3.1	Calcu	late the effective interest rate p.a. correct to three decimal places.	(3)			
8.3	John invest R 120 000. He is quoted a nominal interest rate of 7,2 % per and compounded monthly.						
8.2	An amo years it places.	n amount of R 500 is invested at x % per annum compounded half yearly. After 6 ears it has grown to R 1 126,10. Calculate the value of x , correct to two decimal aces.					
8.1	A new cell phone was purchased for R 7 200. Determine the depreciation value after 3 years if the cell phone depreciates at 25% per annum on reducing balance method. (